

Differences between NPV, Decision Trees, and Real Options

1. NPV is flawed because it systematically undervalues everything due to simplifying assumptions
 - a. Ignores options to expand, extend, contract, abandon and defer projects
 - i. All expected cash flows are pre-committed
 - b. Real option analysis uses decision trees to model optimal actions in the future given the resolution of uncertainty

2. NPV and ROA also deal with mutually exclusive options differently
 - NPV forces pre-commitment to one of many false mutually exclusive decisions, say the decision to defer for one year or two years
 - ROA works backward to arrive at the optimal deferral decision

3. Decision trees make state-contingent future decisions but with a constant discount rate, while ROA changes the discount rate at each branch if necessary
 - Replicating portfolio made up of default-free bonds and a twin security are used to hedge the option

Source: Financial Theory and Corporate Policy, Chapter 9

Risk Measures – Quantile

Definition: α -quantile risk measure is the $(N\alpha)^{th}$ value of the projected liability values

Confidence Interval: $(L_{0(N\alpha-A)}, L_{0(N\alpha+A)})$, where $A = \Phi^{-1}\left(\frac{1+\beta}{2}\right)\sqrt{N\alpha(1-\alpha)}$.

For GMMB, assume $F_k = S_k(1-m)^k$ and stock returns follow lognormal process, then

$$\Pr(G < F_n) = \xi = 1 - \Phi\left(\sigma\sqrt{n} \frac{\log(G/S_0) - n(\mu + \log(1-m))}{\sigma\sqrt{n}}\right)$$

and $V_\alpha = e^{-m}(G - F_0 e^{-z_\alpha \sigma \sqrt{n} + n[\mu + \log(1-m)]})$: quantile risk measure

Quantile Negatives:

- not bounded below by mean loss
- not subadditive
- determined by only one point on loss distribution \rightarrow sampling volatility

Source: *Investment Guarantees*, Chapter 9, pages 159-160, 162, 168-169

The Positive Announcement Effect of Tender Offers on Share Price: Five Separate Hypotheses

| Hypothesis | |
|------------------------------------|--|
| Information or signaling | Positive signal: Firm is expected to have increased future cash flows. Negative signal: Firm has exhausted profitable investment opportunities. |
| Leverage tax shield | If financed via a debt offering, firm leverage increases and so too does the tax shield. |
| Dividend tax avoidance | If more than 20% of a shareholder's holdings are sold back to the firm, the gains from repurchase are treated as capital gains rather than a dividend. |
| Bondholder expropriation | If repurchase reduces asset base of firm, bondholders are worse off because they have less collateral. |
| Wealth transfer among shareholders | Some shareholders will decide not to tender their shares due to different constraints, costs and/or information. |

Source: Financial Theory and Corporate Policy, Chapter 16

Shareholder Rule

$V_N(F)$ = Value of firm's assets after loss before repair

$V_R(F)$ = Value of firm's assets after loss AFTER repair

C = Cost of repair, Assumed $< V_R(F) - V_n(F)$

P_N = Value Default put option with NO asset repair

P_R = Value Default put option WITH asset repair

Shareholder implements repair if:

$$(V_R(F) + P_R) - (V_N(F) + P_N) \geq C \quad \text{i. .e } NPV - P_N + P_R \geq C$$

Source: FET-108-07, Integrated Risk Management page 494

Characteristics of Corporate Debt Markets

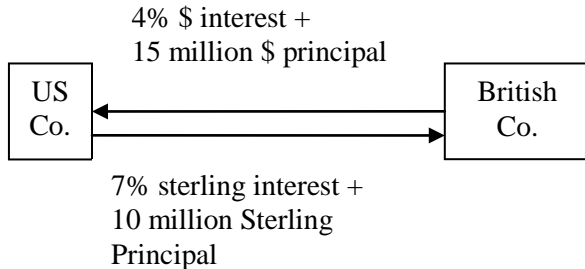
Key Liability Characteristics

1. maturity
2. priority
3. covenants

| Issuer Type | Multinational Issues |
|--|---|
| corporations governments individuals | Eurobonds foreign bonds syndicated loans |
| Maturity | Covenants |
| commercial paper intermediate term long-term bonds | default triggers cash flow controls operating controls strategy controls |

Source: FET-160-08, *Corporate Finance Theory*, Chapter 9, pages 402-408

Currency Swap



Exchange of currency principal is important

Source: Hull, Chapter 7

Analytic Calibration of RSLN

1. Conditional on R_n , the accumulation factor is lognormal with

$$\mu^*(R_n) = R_n\mu_1 + (n - R_n)\mu_2 \text{ and } \sigma^*(R_n) = \sqrt{R_n\sigma_1^2 + (n - R_n)\sigma_2^2}$$

2. The unconditional distribution function $F_{S_n}(x)$ is

$$F_{S_n}(x) = \sum_{r=0}^n \varphi\left(\frac{\log x - \mu^*(r)}{\sigma^*(r)}\right) p_n(r)$$

3. Then input MLE parameters into this analytic distribution function and calculate the resulting quantiles in order to compare them to the calibration points

Source: *Investment Guarantees*, Chapter 4, pages 65-75

Nash Equilibrium (NE) vs. Bayesian Nash Equilibrium (BNE)

| | NE | BNE |
|--------------------|---|--|
| Assumptions | Simultaneous-move game with complete information | Simultaneous-move game with incomplete information |
| Payoffs | $u_i(a_i, a_i) =$ $u_{Chris}(Steak_{Chris}, Red\ Wine_{Pat})$ | $u_i(a_i, a_i; t_i)$ $= u_{Chris}(Steak_{Chris}, Red\ Wine_{Pat}, t_{Chris})$ <p>= Chris's additional private utility for steak and red wine)</p> |
| Def of Strategy | Action rule; ex: in the incomplete Dating game, Chris's strategy was a rule specifying his action for each possible value of t_c . | Action; ex: in the complete Dating game, Chris's strategy was simply to choose steak or chicken. |
| Def of Equilibrium | Pair of strategies such that each player's strategy is the best response to the other player's strategy where "strategy" is defined above for NE. | Pair of strategies such that each player's strategy is the best response to the other player's strategy where "strategy" is defined above for BNE. |

Source: FET-156-08: An Introduction to Applicable Game Theory